# Property-Based Testing for Asynchronous Functional Reactive Programming Using Linear Temporal Logic

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**Abstract.** Functional reactive programming (FRP) is a programming paradigm for implementing software that continuously interacts with its environment and manipulates highly dynamic data. Asynchronous FRP, in particular, is very expressive and can be used to implement graphical user interfaces and other reactive systems interacting with data streams and events that are not synchronized. Testing such asynchronous FRP programs is difficult since a program's behaviour depends not only on the concrete data it receives from its environment but also the *relative timing* of when each piece of data arrives.

In this paper, we propose *PropRatt*, a property-based testing framework for asynchronous FRP. The key component of PropRatt is its specification language, which extends basic linear temporal logic with a means to express properties of several concurrent signals. This allows us to express temporal properties that relate data coming from different signals at different points in time. PropRatt is implemented in Haskell and targets a recently introduced asynchronous FRP language embedded in Haskell. We demonstrate the utility of PropRatt through a case study testing a signal combinator library as well as a graphical user interface, in which we suggest how the strategy for generating signals can be modified to better model specific domains.

**Keywords:** Property-based testing  $\cdot$  Functional Reactive Programming  $\cdot$  Linear Temporal Logic

## 1 Introduction

Reactive systems continuously respond to external inputs received from their environments. Examples of these include graphical user interfaces (GUIs) that react to a stream of mouse-clicks and keyboard inputs, or control software for robots that continuously read input from hardware sensors. The key idea behind functional reactive programming (FRP) [8] is to model the input from the environment as a *signal* that can be manipulated as any other first-class value. This programming paradigm enables writing reactive systems in a declarative and compositional style. In the model of FRP we are considering here, signals are values of type Sig a that represent a stream of values of type a that arrive

time $t_i$	$t_1$	$t_2$	$t_3$	$t_4$	$t_5$	$t_6$	• • •
$s_1 =$	1		2	3	4		
$s_2 =$	'a'	'b'	'c'			'd'	
$\mathtt{zip}s_1s_2 =$	(1, 'a')	(1, 'b')	(2, c)	(3, 'c')	(4, 'c')	(4, 'd')	

Fig. 1. Execution trace for zip.

incrementally over time. These signals can then be composed and manipulated using higher-order functions to build complex reactive systems. Async Rattus [1] is an asynchronous FRP language embedded in Haskell that enables this programming style. The asynchronous nature of the language allows for signals to update independently with respect to a local clock attached to each signal, as opposed to synchronous languages where all signals update according to a global clock. This model is favourable for GUIs, where subcomponents frequently need to be recomputed independently of most of the rest of the GUI. To illustrate such asynchronous behaviour, consider the zip function on signals in Async Rattus (instantiated to signals of integers and characters for the sake of this example):

A call to zip may produce the execution trace illustrated in Figure 1. For each of the three signals, the figure shows a value whenever the signal updates. For example, at time  $t_5$ , the signal  $s_2$  still has value 'c', while the other two signals have been updated to the values 4 and (4, 'c'). The zip function combines two signals into a signal of (strict) pairs containing the two last observed values of the two signals. That means, it must update whenever either of the two argument signals updates. For example, at time  $t_5$ , only signal  $s_1$  updates and  $s_2$  remains unchanged. Accordingly, zip  $s_1$   $s_2$  updates to the new value (4, 'c'). As a sidenote, zip uses the strict pair type operator :\* as Async Rattus is a strict language in order to make guarantees about the absence of space leaks.

From the trace in Figure 1 we can see how the number of test cases explodes. Given two input signals  $s_1$  and  $s_2$  there are  $3^5 = 243$  possible different outcomes for  $zip s_1 s_2$  in the first 6 time steps just due to the different timings of  $s_1$  and  $s_2$ ! And that is before we even begin to consider the number of different values the signals can take. This combinatorial explosion renders conventional unit testing that uses known input/output pairs highly impractical for sufficient testing.

Property-based testing (PBT) [4] is a tool which may aid in addressing these challenges. Instead of writing test cases as input/output pairs, the user specifies a predicate that must hold for all inputs. A testing framework then automatically checks the predicate against many randomly generated inputs, thereby testing a more general property of the system under test. This approach is well-suited for complex or combinatorial input spaces, as it can explore a broad range of inputs that would be impractical to write manually otherwise. To test a representative subset of execution paths, the generation of signals cannot be completely arbi-

<sup>&</sup>lt;sup>1</sup> Int :\* Char denotes a strict pair type of integers and characters.

trary. Instead, it must be carefully constrained to ensure fairness for all signals under test, to avoid a signal never updating during a test run.

However, predicates written exclusively with propositional logic are insufficiently expressive to specify the expected behaviour of signals, as it can only represent a static notion of truth. The value produced by a signal at a given instant is of limited use, since it cannot express how signals evolve dynamically over time. This naturally leads us to temporal logic, which allows properties to be formulated with temporal operators. In particular, linear temporal logic (LTL) [16] provides operators such as  $\mathbf{G}$  ("always") and  $\mathbf{F}$  ("eventually") to express statements relative to time. For example, we can express the property that the first component of a zipped signal  $s_3 = \mathbf{zip} \, s_1 \, s_2$  always reflects the current value of  $s_1$  whenever  $s_1$  produces a value:

$$\mathbf{G}(\checkmark s_1 \to s_1 = fst(s_3)) \tag{1}$$

Here,  $\sqrt{s_1}$  denotes a tick of the clock tied to  $s_1$ , capturing the idea that the property is only relevant when  $s_1$  updates. Using the temporal operators offered by LTL allows for more expressive predicates and, in turn, properties of a system that we wish to test. Exactly how an LTL-based specification language should be designed to express specifications for *asynchronous* FRP has remained an open question so far.

In this paper we present PropRatt<sup>2</sup>, a property-based testing (PBT) library for Async Rattus. PropRatt builds on top of QuickCheck [4], a PBT library for Haskell, to generate arbitrary signals and to check temporal properties. The key contributions of this work are as follows:

- We devise an LTL-based specification language to express temporal properties that involve multiple asynchronous signals.
- We implement an API that allows specifications to interact with several signals of heterogeneous types in a type-safe manner using Haskell's advanced type system features.
- We combine this API with an execution model that produces finite welltyped traces of parallel, asynchronous signals.
- We implement a testing harness that integrates the specification language and execution model into QuickCheck.
- We demonstrate the expressiveness of the specification language, its use, and its limitations in practice with a number of examples.

The remainder of this paper is structured as follows: In section 2 we give a short introduction to the Async Rattus language and property-based testing. In section 3 we present the LTL-based specification language, and in section 4 we give an extended example of its use in PropRatt. In section 5, we give an overview of the most important parts of the implementation of PropRatt and its specification language. Finally, we give an overview of related work in section 6 and conclude in section 7 with an outlook on future work.

<sup>&</sup>lt;sup>2</sup> Source code of Haskell package and examples submitted as supplemental material.

# 2 Background

In this section, we give a brief introduction to functional reactive programming in the Async Rattus language and property-based testing.

Async Rattus Async Rattus is an FRP language embedded in Haskell that enables programming with asynchronous signals. It uses modal types to reflect the temporal availability of expressions and values at the type level. To this end, Async Rattus introduces two type modalities: a later modality 0, and a box modality Box. The later modality defers a computation to a future time step, while the box modality classifies time-independent data that can be moved unchanged across time. By encoding timing constraints at the type level, Async Rattus guarantees that only time-appropriate values are accessed at each step. For example, a computation cannot accidentally use a value before it is received at some later time. But these modalities also aid resource management: The runtime only needs to keep the current values and the deferred computations awaiting future input, freeing any older data that is no longer needed, thus avoiding space leaks, which are notoriously difficult to debug. The core FRP abstraction provided by Async Rattus is the signal type. A signal of type Sig a represents a (possibly infinite) stream of values of type a. It is defined in Async Rattus as a recursive type:

data Sig a = a ::: 0 (Sig a)

Here we use ::: as a cons-like constructor. A value of type Sig a carries an immediate head of type a and a tail of type O (Sig a). The head is available right away, while the tail is a computation that becomes available in the next time step, according to some clock.

Each value d:: 0 b consist of a *clock* cl(d) and a delayed computation, which produces a value of type b whenever the clock cl(d) ticks. In the case of a signal, the tail is of type 0 (Sig a) and thus has an associated clock, which determines when a new value of type Sig a is available, i.e. when the signal updates. Concretely, a clock is simply a set of external input channels. When an input arrives on one of those channels, we say that the associated clock ticks and the deferred computation is executed. In the case of the tail of a signal, such a tick yields the next value of the signal. Thus, each 0 (Sig a) is essentially a promise to compute the next signal element as soon as the clock ticks. For example, if a signal's clock includes a GUI button's event channel, then each button press causes the signal to advance by one step. This design lets different signals operate on independent clocks, unlike purely synchronous FRP where all signals share a single global clock.

Async Rattus provides two primitives for working with the later modality: delay and adv (advance). The delay keyword is the constructor for the later modality. It wraps a computation so that it does not execute until the signal's clock ticks. Conversely, adv is the eliminator. It retrieves the value from a delayed computation when its clock allows it. The typing rules of Async Rattus

ensures that every adv must be nested under the scope of a corresponding delay, preventing the use of values that do not exist.

For instance, consider the following function, that subtracts one from a delayed integer:

```
subtractOne :: 0 Int -> Int
subtractOne laterN = laterN - 1
```

This function does not type check since laterN :: 0 Int is not an integer but rather a delayed integer that arrives at some point in the future. We cannot subtract 1 in the current time step. Instead, we have to await the clock of the integer and only then subtract 1. A valid function could instead use the delay and adv primitives to delay the computation according to the clock of laterN.

```
subtractOne :: 0 Int -> 0 Int
subtractOne laterN = delay (adv laterN - 1)
```

In this way, we correctly await the input, before executing the computation, which naturally also changes the type of the function, to return a delayed integer.

Async Rattus requires that any value moved into the future be time-invariant, introducing the notion of stable types. Values of stable types are time-independent and consequently can be safely moved arbitrarily far into the future without risk of space leaks. To illustrate, consider a naive map implementation on signals:

```
mapNaive :: (a -> b) -> Sig a -> Sig b
```

This type is naive because function types are inherently not stable, as they may capture temporally-dependent information in their closure.

Instead, map can be defined as:

```
map :: Box (a -> b) -> Sig a -> Sig b
```

The box modality ensures the function is stable and thereby guaranteed temporally-invariant. This ensures that no new time-varying information is hidden inside the function, ensuring an absence of space leaks.

Property-Based Testing Testing reactive and asynchronous programs written in Async Rattus is challenging because of the enormous space of possible event sequences. Property-based testing (PBT) offers a promising alternative to traditional testing. Instead of writing fixed test cases, the programmer states properties that the program should satisfy, and the testing framework checks them against many automatically generated inputs. This approach aligns well with the high-level nature of specifications and can uncover edge cases that handwritten examples might miss. PBT libraries allow the programmer to write compact specification, such as the following specification that reversing a list twice produces the original list

```
prop_rev : [Int] -> Property
prop_rev xs = reverse (reverse xs) == xs
```

```
Predicate \varphi ::= T \mid F \mid e \mid \neg \phi \mid \phi \land \psi \mid \phi \lor \psi \mid \phi \Rightarrow \psi
\mid \mathbf{X} \phi \mid \mathbf{F} \phi \mid \mathbf{G} \phi \mid \phi \mathbf{U} \psi \mid \phi \mathbf{R} \psi
Expression e ::= c \mid e_1 \mid e_2 \mid l \mid \checkmark l
Lookup \mid l ::= \mathbf{prev} \mid l \mid \mathbf{sig}_n
```

Fig. 2. Syntax of PropRatt's specification language.

A PBT library such as *QuickCheck* can generate random inputs for the argument xs and check whether these satisfy the equation reverse (reverse xs) == xs. In addition, QuickCheck also can also *shrink* such inputs in order to provide the programmer with useful counterexamples if a property fails.

The core of this general principle is provided by the Arbitrary type class of QuickCheck:

```
class Arbitrary a where
  arbitrary :: Gen a
  shrink :: a -> [a]
```

Given an instance of Arbitrary [Int], QuickCheck can test properties that quantify over lists of integers such as prop\_rev above: First arbitrary generates random values of type [Int]. Then it supplies these random values to the function prop\_rev one by one. Finally, if the property fails for one of the generated inputs, say xs, then shrink xs will produce smaller lists with which to test prop\_rev in order to obtain a smaller counterexample.

In the context of reactive systems, PBT can offer the same benefits: It can generate arbitrary input signals to explore the space of behaviours and shrink such signals to simpler counterexamples to help locate the source of errors. However, equational specifications alone are not sufficiently expressive to capture the complex behaviours expressible by asynchronous FRP programs.

## 3 Specification language

# 3.1 Untyped specification language

PropRatt introduces a DSL for writing declarative specifications at a high level of abstraction, enabling property-based testing of FRP programs written in Async Rattus. Such programs manipulate signals of different types, e.g. zip from section 1 combines an Int and a Char signal. Therefore, the design of the specification language must be able to account for multiple, heterogeneously typed signals. But before turning to the concrete syntax of the typed specification language as implemented in PropRatt, we consider an idealized syntax of an untyped version of the language in Figure 2 in order to discuss the essential ideas of the language.

The specification language consists of three components: a logical language of predicates  $\phi$ , a language of expressions e, and a notation l for looking up

signals at a specific (relative) time. The predicate language is exactly LTL with atoms of the form e written in the expression language. For example, we write  $\mathbf{G}(\mathbf{sig}_1>0)$  to express that the signal identified by  $\mathbf{sig}_1$  always (globally) has a positive value, and we write  $\mathbf{sig}_1>0$  U  $\mathbf{sig}_1=\mathbf{sig}_2$  to express that the signal  $\mathbf{sig}_1$  is positive until both  $\mathbf{sig}_1$  and another signal  $\mathbf{sig}_2$  have the same value.

In these examples,  $\mathbf{sig}_1 > 0$  and  $\mathbf{sig}_1 = \mathbf{sig}_2$  are Boolean-valued expressions, which can act as atoms in an LTL formula. In general, an LTL formula is a predicate over n signals whose current value can be referenced using  $\mathbf{sig}_1 \dots \mathbf{sig}_n$ . We can also reference a previous value of a signal by using  $\mathbf{prev}$ . For example,  $\mathbf{G}(\mathbf{X}(\mathbf{prev}\ \mathbf{sig}_1 < \mathbf{sig}_1))$  stipulates that signal  $\mathbf{sig}_1$  is strictly monotonically increasing.

Traditionally, LTL works only on a *single* execution trace, whereas PropRatt allows multiple parallel signals, which may produce new values independently of one another according to their own clock. However, given such parallel, asynchronous signals, we can construct a single execution trace that maintains the relative timing information. We have seen an example of that in the execution trace for zip, shown in Figure 1. It involves three signals, which, if combined, produce a trace where at each time step  $t_i$  at least one of the three signals ticks, i.e. produces a new value.

In the expression language we have access to the timing information of such a combined trace via expressions of the form  $\checkmark s$ , which are true whenever the signal identified by s has ticked. Returning to the zip example from Figure 1, we have that at time  $t_5$ , the expressions  $\checkmark sig_1$  and  $\checkmark sig_3$  are true, since both  $s_1$  and  $zip s_1 s_2$  produced a new value, whereas  $\checkmark sig_2$  is false as  $s_2$  did not produce a new value. Using this more formal notation for the specification language, specification (1) is written more precisely as  $\mathbf{G}(\checkmark sig_1 \rightarrow sig_1 = fst \lq sig_3)$ , where  $fst \lq$  is the first projection of the strict pair type.

To illustrate the specification language, suppose we have a GUI with the following signals:

The timer signal is meant to increment by one every second and reset produces a unit value () every time the 'reset' button in the GUI is pressed. Assume that the signals we wish to test are supplied in the order they appear above, i.e.  $\mathbf{sig}_1 = \mathbf{timer}$  and  $\mathbf{sig}_2 = \mathbf{reset}$ , we can specify that timer increments whenever the clock of timer ticks and the reset button is not pressed:

$$\mathbf{G}(\sqrt{\operatorname{sig}}_1 \wedge \neg \sqrt{\operatorname{sig}}_2 \Rightarrow \mathbf{X}(\operatorname{prev} \operatorname{sig}_1 < \operatorname{sig}_1) \tag{2}$$

Here **G** and **X** are the standard LTL temporal operators. The expression  $\checkmark \operatorname{sig}_1$  retrieves whether the first signal has updated in the current time step as an expression, while  $\operatorname{sig}_1$  retrieves the value of that signal. The lookup  $\operatorname{prev} \operatorname{sig}_1$  accesses the value of the timer from the previous time step. The property asserts that at any time (**G**), whenever the timer signal ticks ( $\checkmark \operatorname{sig}_1$ ), then in the next step (**X**) the timer ( $\operatorname{sig}_1$ ) must have increased relative to its previous value

```
data Pred (ts :: [Type]) where
 TT, FF
                      :: Pred ts
 Now
                      :: Expr ts Bool -> Pred ts
 Not, X, G, F
                      :: Pred ts -> Pred ts
 And, Or, (:=>), U, R :: Pred ts -> Pred ts
data Expr (ts :: [Type]) (t :: Type) where
      :: t -> Expr ts t
 Pure
 App
        :: Expr ts (t -> r) -> Expr ts t -> Expr ts r
 Val
        :: Lookup ts t -> Expr ts t
 Tick :: Lookup ts t -> Expr ts Bool
data Lookup (ts :: [Type]) (t :: Type) where
 Prev :: Lookup ts t -> Lookup ts t
 Sig1 :: Lookup (Value t ': x) t
 Sig2 :: Lookup (x1 ': Value t ': x2) t
```

Fig. 3. Well-typed syntax of PropRatt.

(**prev**  $\mathbf{sig}_1$ ). Importantly, this is only the case if reset has not been pressed  $(\neg \checkmark \mathbf{sig}_2)$ .

#### 3.2 Typed specification language

The syntax in Figure 2 is untyped and to ensure well-typedness we have to give a type system so that only Boolean-valued expressions are used as atoms, and expressions themselves are also well-typed, e.g.  $e_1 e_2$  is only well-typed if  $e_1$  is of type  $\tau_1 \to \tau_2$  and  $e_2$  is of type  $\tau_1$ . Instead of presenting such a type system, we give the encoding of this type system in Haskell.

The concrete syntax of PropRatt's specification language is intrinsically well-typed and uses generalized algebraic data types (GADTs) to represent the typing information. The full definition of the syntax is given in Figure 3. The type of predicates Pred is indexed by a list of type ts :: [Type], which represents the types of the signals over which we want to specify a property. For example, for the property involving the timer :: Sig Int and reset :: Sig () signals, this list of types is '[Int,()].

Similarly, expressions are indexed by such a list of types ts :: [Type], as well. But they also have an additional type index t :: Type that indicates the type of values produced when evaluating such expressions. Using the Now constructor, predicates over signal types ts may include expressions of type Bool over signal types ts. In turn, expressions have access to the values and timing information of the signals via Val and Tick, respectively. In addition, they also have an applicative functor structure provided by Pure and Apply. These two constructors correspond directly to the two operations pure and <\*>

```
sig1 :: Expr (Value t ': ts) t
sig1 = Val Sig1
tick1 :: Pred (Value t ': ts)
tick1 = Now (Tick Sig1)
-- sig2, tick2, etc. are defined similarly
prev :: Expr ts t -> Expr ts t
prev (Pure x) = Pure x
prev (App f x) = App (prev f) (prev x)
prev (Val lu) = Val (Prev lu)
prev (Tick lu) = Tick (Prev lu)
instance Num t => Num (Expr ts t) where
  (+) x y = (+) < x < y
  -- similar definitions for (-), (*) etc
(|<|) :: Ord t => Expr ts t -> Expr ts t -> Pred ts
x \mid < \mid y = Now ((<) < x <*> y)
-- similar definitions for comparison operators (==), (<=) etc.
```

Fig. 4. Shorthand notations for the specification language.

of the applicative functor interface. For example the expression  $\mathbf{prev} \, \mathbf{sig}_1 < \mathbf{sig}_1$  from the timer specification (2) above, is written

```
(<) <$> Val (Prev Sig1) <*> Val Sig1
```

where \$ is the map operator of applicative functors, defined by f \$ x = pure f \$ x. The above expression is of type Expr '[Int,()] Bool and thus can be used in a predicate using Now. The type of the Sig1 constructor ensures that the type of Index Sig1 matches exactly the first signal, and likewise for the remaining constructors Sig2 etc.

Putting all of this together, specification (2) can be expressed as follows:

To make properties more readable, the specification language also provides shorthands, defined in Figure 4. This includes shorthands for looking up the current value of a signal (sig1, sig2 etc.), checking whether a signal has ticked (tick1, tick2 etc.), Prev generalized to the expression language (prev), common arithmetic operators for the expression language, and common comparison operators for the predicate language (|<|,|==| etc.). With these shorthands the above property prop can be written more concisely:

```
prop :: Pred '[Int,()]
prop = G ((tick1 'And' Not tick2) :=> X (prev sig1 |<| sig1))</pre>
```

## 4 Case study

To evaluate the expressiveness of the specification language, we have compiled two sets of example specifications: A set of specifications for the signal combinators provided by the Async Rattus library and a set of specifications for a simple timer GUI. Here we give a selection of these specifications, but the complete set can be found in the supplemental material submitted with this paper.

**Signal combinators** The first set of examples comprises specifications for signal combinators like zip and map. We have seen one such specification in the form of the LTL formula  $G(\sqrt{sig_1} \to sig_1 = fst', sig_3)$  for the zip combinator. This can be written in the typed specification language as follows:

```
-- sig3 = zip sig1 sig2
prop_zip1 :: Pred '[Int, Char, (Int :* Char)]
prop_zip1 = G (tick1 :=> (sig1 |==| (fst' <$> sig3)))
```

Async Rattus can express dynamic dataflows using the switch combinator, which takes a signal s1 and a delayed signal s2 and produces a new signal that first behaves like s1 and behaves like s2 as soon as that delayed signal s2 arrives. We can express this property as follows:

```
-- sig3 = switch sig1 sig2
prop_switch :: Pred '[Int, Int, Int]
prop_switch = (sig3 |==| sig1) 'U' (tick2 'And' G(sig3 |==| sig2))
```

Note that PropRatt's until operator U has the semantics of the 'weak until' operator (often denoted W). In an LTL formula  $\phi$  U  $\psi$ , the 'strict until' operator requires  $\psi$  to become true at some point in the future (and  $\phi$  to be true at all times before that). However, this requirement of  $\psi$  becoming true at some point is a liveness property, which cannot be tested using PBT since such properties have only infinite counterexamples. Therefore, by necessity, PropRatt adopts the weak form which does not require  $\psi$  to become true. This 'weak until' semantics of U matches the semantics of switch because the second (delayed) signal passed to switch may never arrive.

**GUI application** For the second set of example specifications, we consider a GUI application that extends the timer example from section 3.1 to include additional signals. This GUI application is taken from Disch et al. [7] and implements the timer of Kiss's 7GUIs benchmark [12].

The timer application displays a value of elapsed time e, a reset button r and a slider for adjusting a maximum duration d. Users may interact with the timer in two ways: pressing the reset button and adjusting the slider which changes the

maximum value the timer may reach. Once the timer reaches this maximum, it stops incrementing until the slider is moved again or the reset button is pressed. The GUI processes three inputs: a reset button (reset :: Sig ()), a slider to adjust the maximum of the timer (max :: Sig Int), and a signal that ticks every second (sec :: Sig ()). These three signals are combined to form the signal of type state:: Sig (Int :\* Int), which captures the state of the GUI. Its first component holds the current timer value and its second component is the maximum value currently chosen by the user.

Kiss [12] provides a specification of the timer application consisting of several informal properties, which we can now formally express in the PropRatt specification language. First, the timer must stop whenever it reaches its maximum. That is, the timer value never exceeds the maximum value supplied by the user:

```
-- sig1: state; sig2: reset; sig3: max; sig4: sec
prop1 :: Pred '[(Int :* Int), (), Int, ()]
prop1 = G ((snd' <$> sig1) |<=| sig3)</pre>
```

Second, if the timer has not yet reached its maximum, then it must increase every second:

Third, whenever the user presses the reset button, then in that same time step the timer value must be 0:

```
prop3 :: Pred '[(Int :* Int), (), Int, ()]
prop3 = G (tick2 :=> (pure 0 |==| (fst' <$> sig1)))
```

Finally, implicit in the specification of the timer GUI is the property that the timer should remain constant unless a second has passed or the reset button was pressed:

Testing of these properties confirms that the implementation of the timer GUI by Disch et al. [7] does indeed satisfy the specification.

# 5 Implementation

In section 3, we introduced the key type Pred, which defines well-typed temporal specifications. We now turn to the implementation details that connect these specifications to property-based testing with QuickCheck [4].

A specification is evaluated using the following function:

```
evaluate :: Pred ts -> Sig (HList ts) -> Bool
```

The type Sig (HList ts) represents a flattened trace of a program containing data from all signals under test such as the example trace for zip in Figure 1. Understanding this type requires a short detour into how asynchronous signal behaviour is represented. A naive approach might model a trace as a list of independent signals [Sig a]. This representation is insufficient as it does not allow us to inspect the timing relationships between signals directly. Instead, we want a single signal of lists, where the nth value in a list corresponds to the value produced by the nth signal of the property we are testing. In order to also represent cases where some of the signals do not produce a new value, we can represent such a single signal with the type Sig [Maybe a]. This representation is essentially the idea of the type Sig (HList ts) used by evaluate above, but instead of a list it uses a heterogeneous list type (HList) that allows different signals to have different types:

```
data HList :: [Type] -> Type where
  HNil :: HList '[]
  (:%) :: !x -> !(HList xs) -> HList (x ': xs)
```

Users can construct a heterogeneous list of signals to test:

```
-- assuming s1 :: Sig Int, s2 :: Sig Char
sigsOfZip :: HList '[Sig Int, Sig Char, Sig (Int :* Char)]
sigsOfZip = s1 :% s2 :% zip s1 s2 :% HNil
```

Such a heterogeneous list of signals is then flattened into a single signal that can then be passed to evaluate:

```
traceOfZip :: Sig (HList '[Value Int, Value Char, Value (Int:*Char)])
traceOfZip = flatten sigsOfZip
```

Before looking more closely at flattening, we take a look at the Value type.

To support operators such as  $\checkmark$  and **prev**, the trace must maintain past values and indicate whether a signal has emitted a fresh value at the current time step. We collect this data in the Value type:

newtype HasTicked = HasTicked Bool deriving Show

```
data Value a = Current !HasTicked !(List a)
```

Recall the definition of the Lookup type in Figure 3 that represents lookups of signal values. The type of each Sign constructor enforces that the nth type in the list of types ts is of the form Value t in the type signature of evaluate.

To illustrate this representation, we show the trace from Figure 1 as a value of type Sig (HList '[Value Int, Value Char, Value (Int :\* Char)]):

At  $t_0$ , both signals produce a new value, whereas at  $t_1$ , only the second signal emits a new value while the first carries over its previous one, which is also indicated by the false Boolean flag at  $t_1$ .

Flattening of signals to traces To construct traces from individual signals, we define the function prepend, which merges a signal Sig t with an already-flattened signal of heterogeneous list Sig (HList ts):

The key idea is that prepend unions the clocks of the delayed computations from both arguments, which means the resulting signal updates whenever either of the input signals would update. This enables us to explore traces systematically. The Stable constraints ensures that the values produced by either signal argument are temporally-independent and safe to move to the future according to the type system of Async Rattus, and Falsify is a type class that implements a single method for a Value to negate the HasTicked flag. To flatten a heterogeneous list of signals to a trace, we recursively apply prepend through the flatten method defined in the multi-parameter type class Flatten:

```
class Stable (HList vals) =>
  Flatten sigs vals | sigs -> vals, vals -> sigs where
    flatten :: HList sigs -> Sig (HList vals)

instance Flatten '[] '[] where
  flatten HNil = emptySig

instance (Stable a, Stable (Value a), Flatten as bs, Falsify bs)
  => Flatten (Sig a ': as) (Value a ': bs) where
  flatten (HCons h t) = prepend h (flatten t)
```

We use a type class to implement flatten so that we can express the relation between the argument type HList sigs and return type Sig (HList vals). Namely, sigs is a list of types of the form Sig t, whereas vals is the corresponding list of types of the form Value t. The type class declaration uses functional dependency annotations to make explicit that sigs and vals are in a one-to-one correspondence, which helps the type checker to infer types.

Clock strategy The clock of a delayed computation is represented by a set of so-called *channels* [2]. For example, the clock  $\{\kappa_1, \kappa_2\}$  indicates that it will tick if data arrives on channel  $\kappa_1$  or channel  $\kappa_2$ . Clocks such as  $\{\kappa_1, \kappa_2\}$  and  $\{\kappa_2, \kappa_3\}$  may tick simultaneously if data has arrived on a channel that both share, in this case  $\kappa_2$ . Concretely, channels are represented as integers in Async Rattus, so that clocks are represented using the type IntSet of finite sets of integers.

PropRatt must generate clocks in a manner that adequately reflects asynchronous behaviour when signals are combined. During evaluation of properties in PropRatt, we advance the state of the signals under test controlled by evaluation semantics of the specification language. This advancement must update those signals that produce a new value while preserving the values of signals that do not. To realize this behaviour, we randomly assign each delayed computation of a generated signal a clock drawn from the non-empty subsets of  $\{\kappa_1, \kappa_2, \kappa_3\}$ :

```
genClock :: Gen Clock
genClock = do
   n <- chooseInt (1, 3)
   case n of
   1 -> do x <- chooseInt (1,3)
        return (IntSet.fromList [x])
   2 -> elements $ map IntSet.fromList [[1,2], [2,3], [1,3]]
   3 -> return (IntSet.fromList [1,2,3])
```

During the evaluation of the test, we then advance the signals by forcing the delayed computation on the smallest channel of its clock. Together with the implementation of prepend which unions the clock of each delayed computation upon merge, this strategy makes it possible to produce both synchronous ticks, where signals updates at the same time because the clocks share channels, but also asynchronous advancements in which some signals wait multiple time steps before advancing.

This extension allows us to generate arbitrary input signals that mimics asynchronous user interaction, combine them with user-supplied signals if desired, and integrate the resulting outputs into a model of our program.

**Shrinking** We supply implementations of the **shrink** method given by the **Arbitrary** type class from QuickCheck. We implemented a shrinker for signals by converting signals into a list that preserves the clocks of delayed computations:

```
type TSig a = [(a, Clock)]
```

This representation allows us to shrink signals using a strategy similar to that for lists implemented in QuickCheck: Shrink the signal by iteratively dropping contiguous chunks of values and shrink the remaining values contained in the signal themselves as well. After producing new shrink candidates, we rebuild them as signals and reapply the saved clocks so the delayed-computation strategy is preserved. QuickCheck evaluates shrink candidates iteratively until the property no longer fails. This yields compact failing inputs and correspondingly short traces that help pinpointing errors in the implementation or the specification.

#### 6 Related work

LTL has long been recognized as a suitable specification language for reactive programs. Jeffrey [10] and Jeltsch [11] independently discovered that LTL can

be seen as a type system for functional reactive programs. Later, Perez and Nilsson [14,15] used LTL as a specification language for property-based testing of functional reactive programs. LTL-based specification languages have also been used for property-based testing of web applications [13]. The work most closely related to PropRatt is the property-based testing library developed for Rattus [6], a synchronous version of Async Rattus.

In all previous work mentioned above, the LTL-based specification language always targets single, synchronous executions of programs. By contrast, PropRatt specifications are hyperproperties, i.e. properties over several parallel execution traces of signals. Variants of LTL for hyperproperties have been suggested [5], but we are not aware of any property-based testing framework that uses these ideas, apart from the thesis of Nielsen and Kristiansen [3] which this paper summarizes. However, we are not the first to devise a specification language for PBT of asynchronous reactive systems. Hughes et al. [9] have proposed temporal relations as a specification language for testing the asynchronous behaviour of a communication protocol. A temporal relation is a relation between time intervals and values. Such relations provide a compositional way to specify properties of asynchronous computations.

#### 7 Conclusion and Future Work

We have presented an LTL-based specification language that enables PBT of asynchronous FRP programs. To our knowledge this is the first such PBT specification language that combines LTL-style connectives with the ability to express properties across multiple asynchronous signals.

The focus of the present work is to explore the expressiveness of asynchronous LTL specifications and to demonstrate it with case studies. This leaves considerations of ergonomics of the specification language for future work. Such considerations are important, because the ease with witch specifications can be written, read, and modified do significantly contribute to the utility of a PBT framework. The design of PropRatt as a hybrid DSL with a deeply embedded core allows for further improvements to the specification language. For example, by inspecting the AST of specifications, we can produce a warning when the user tries to test liveness properties, which by their nature do not have finite counterexamples and thus cannot be tested.

In addition, we could extend the language with further connectives. For example, the predicate fragment of the specification language has combinators that move forward in time (such as **X** and **U**), whereas the expression fragment has a combinator that moves backwards in time (namely **prev**). While this design decision simplifies the implementation of an efficient checking procedure for specifications, it can lead to unnatural or inelegant specifications. However, it is possible to extend the specification language with combinators that allow e.g. the expression fragment to also move forward in time. Specifications written in this richer specification language can then be translated into an equivalent specification in the simpler specification language presented in this paper.

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